

## B.S.T.J. BRIEFS

### Quantum Efficiency of the Green and Red Electroluminescence of GaP

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Gallium phosphide crystals were grown from polycrystalline material in a solution of gallium contained in evacuated and sealed-off quartz tubes.<sup>1</sup> For the regrowth, the tube with the GaP-Ga mixture was heated to 1250°C and cooled at a rate of 1.5°C per minute. After separation of the GaP crystals from the adherent Ga, Zn was diffused into the crystals,

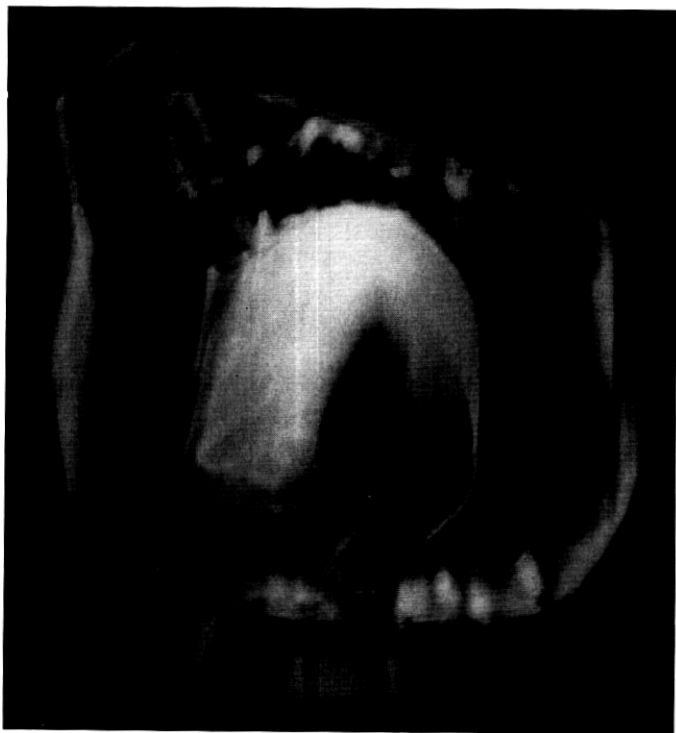


Fig. 1 — Red electroluminescent gallium phosphide crystal photographed in its own light; p-n junction prepared by diffusion of Zn at 800°C for four hours. Length of the straight side of the crystal about 1.5 mm.

leading to red (7000 Å) electroluminescent junctions. The diffusion was done in an evacuated and sealed-off quartz tube using as a source<sup>2</sup> a Zn + GaP mixture. The efficiency of the emission was determined with an integrating sphere and a photomultiplier with S-1 response calibrated in absolute units, and was found at room temperature to be about  $1.0 \times 10^{-3}$  photons per electron for the best samples. Red electroluminescence in GaP was previously reported to have efficiencies of about  $10^{-4}$  (see Ref. 3) and  $10^{-4} - 10^{-3}$  (see Ref. 4).

If silver contacts are alloyed onto the rough side of the solution-grown GaP crystals, green electroluminescence can frequently be observed at the contact area. The efficiency of the green emission was found to be  $4 \times 10^{-5}$  photons (5550 Å) at 300°K observed outside the crystal per recombining electron-hole pair for the best samples. This compares with efficiencies of  $3 \times 10^{-5}$  measured by Gershenzon et al.<sup>5</sup> and efficiencies smaller than  $10^{-4}$  as indicated by Allen et al.<sup>3</sup>

The figure shows one of the red electroluminescent crystals with a Zn-diffused junction photographed in its own electroluminescent light.

#### REFERENCES

1. Wolff, G., Keck, P. H., and Broder, J. D., *Phys. Rev.*, **94**, 1954, pp. 753-754.
2. Foy, P. W., private communication.
3. Allen, J. W., Moncaster, M. E., and Starkiewicz, J., *Solid-State Elect.*, **6**, 1963, pp. 95-102.
4. Gershenzon, M., and Mikulyak, R. M., *Solid-State Elect.*, **5**, 1962, pp. 313-329.
5. Gershenzon, M., Mikulyak, R. M., Logan, R. A., and Foy, P. W., to be published in *Solid-State Elect.*

## Matching of Optical Modes

By H. Kogelnik

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In experiments with coherent laser light it is frequently necessary to transform a given Gaussian beam<sup>1,2</sup> into a Gaussian beam with certain desired parameters. It is required, for example, to transform the light beam emerging from a laser oscillating in a fundamental mode in order to provide for optimum injection into a light transmission line<sup>2,3</sup> (consisting of a sequence of lenses), or for optimum coupling into a spherical mirror interferometer.<sup>4</sup> In these cases one has to "match" the incoming beam to the natural mode of the system in question. Lenses inserted in the beam perform the matching transformation. The design of a match-

ing configuration has to take full account of the laws<sup>1,2,3</sup> that govern optical modes. This leads to a somewhat complex analysis.<sup>5</sup> The results, however, are quite simple matching formulae which are presented in this brief. A matching experiment is described for illustration.

The given beam is characterized by its minimum beam radius<sup>1,6</sup> (spot size)  $w_1$  and by the location of the beam waist. The problem is to transform this beam into another with a minimum radius  $w_2$ . The quantities  $w_1$  and  $w_2$  determine a characteristic "matching length"  $f_0$  given by

$$f_0 = \pi \frac{w_1 w_2}{\lambda} \quad (1)$$

where  $\lambda$  is the wavelength. One beam is transformed into the other if a lens with a focal length  $f$  larger than  $f_0$  is spaced between the two beam minima as shown in Fig. 1. The distances  $d_1$  and  $d_2$  between the lens and the beam minima have to satisfy the following matching conditions

$$\frac{d_1}{f} = 1 \pm \frac{w_1}{w_2} \sqrt{1 - \frac{f_0^2}{f^2}} \quad (2)$$

$$\frac{d_2}{f} = 1 \pm \frac{w_2}{w_1} \sqrt{1 - \frac{f_0^2}{f^2}} \quad (3)$$

where the same sign should be used in both equations. From (2) and (3) it follows that matching is not possible if  $f < f_0$ . If one chooses  $f = f_0$  then  $d_1 = f_0$  and  $d_2 = f_0$ ; the beam minima are located in the two focal planes of the lens.

When one uses more than one lens to achieve the desired beam transformation, the above matching formulae are still applicable. Then  $f$  is the focal length of the lens combination, and  $d_1$  and  $d_2$  are measured from the principal planes. If the modes of two given optical systems are to be matched, one need not evaluate the beam parameters  $w_1$  and  $w_2$ , which are functions<sup>1,6</sup> of  $\lambda$  and the system parameters: the matching param-

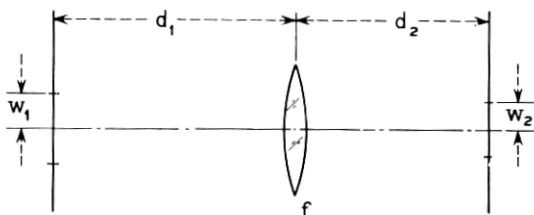


Fig. 1 — Matching configuration.

ters  $f_0$ ,  $\frac{w_1}{w_2}$ ,  $d_1$ , and  $d_2$  are independent of  $\lambda$  and can be expressed in terms of the system parameters alone.

In our experimental study the light beam was taken from a He-Ne gas laser oscillating in a fundamental mode at  $\lambda = 0.63$  micron. The laser cavity consisted of a concave mirror of 1 meter focal length and a flat output mirror. The mirror spacing was 1.7 meters. The (minimum) beam radius at the flat is computed<sup>1</sup> as  $w_1 = 0.37$  mm. This beam was passed through a matching lens and then injected through a slit into a mirror system formed by two concave mirrors of 12.5 meters focal length

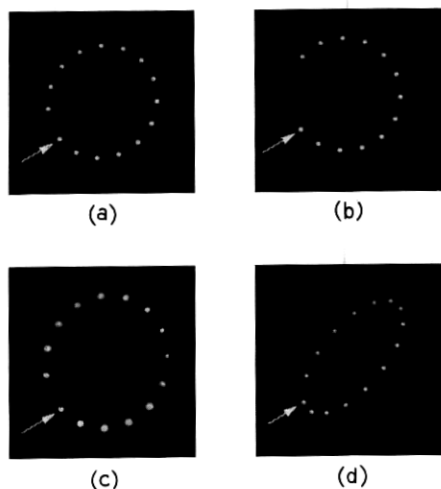


Fig. 2 — Photographs of beam spots on mirror.

spaced 50 centimeters apart. The injection angle was so chosen that the beam was reflected back and forth between the mirrors many times before it was finally intercepted, with the points of beam impact on each mirror forming a circular pattern. Such a beam configuration was described and analyzed in Ref. 7. As the beam passes back and forth between the mirrors its radius is changed in the same way as for transmission through a sequence of lenses<sup>2,3,8</sup> with corresponding parameters. The minimum beam radius of a fundamental mode of this sequence is computed as  $w_2 = 0.7$  mm.

From the above data one obtains a matching length of  $f_0 = 1.3$  meters. A lens of a focal length of  $f = 1.3$  meters was available and was used as

matching lens. Therefore, spacings  $d_1 = d_2 = f_0 = f = 1.3$  meters were required for matching.

A mirror of the multiple-pass system was slightly transparent and Fig. 2 shows photographs of the beam-impact points taken through this mirror. In Fig. 2(a) the arrow marks the point where the injected beam strikes the mirror first. After one return trip the point of impact is the neighboring point to the right. Subsequent impact points after a corresponding number of return trips appear counterclockwise on a circle. The beam was intercepted after 14 return trips. For illustration we show Fig. 2(b), where the beam was intercepted after 12 return trips. In both cases mode-matching conditions were fulfilled and all beam radii at impact are seen to be the same. In Fig. 2(c) one can see how the beam radii at the mirror vary periodically<sup>9</sup> if some mismatch is introduced: the spacing  $d_1$  was misadjusted by about 25 cm. Fig. 2(d) shows the elliptical pattern obtained for another injection angle. Here the modes were matched again and all beam spots are of equal size.

#### REFERENCES

1. Boyd, G. D., and Gordon, J. P., Confocal Multimode Resonator for Millimeter Through Optical Wavelength Masers, B.S.T.J. **40**, March, 1961, pp. 489-508.
2. Goubau, G., and Schwering, F., On the Guided Propagation of Electromagnetic Wave Beams, I.R.E. Trans., **AP-9**, 1961, pp. 248-56.
3. Pierce, J. R., Modes in Sequences of Lenses, Proc. Nat. Acad. Sci. **47**, 1961, pp. 1808-31.
4. Fork, R. L., Gordon, E. I., Herriott, D. R., Kogelnik, H., and Loofbourrow, J. W., Scanning Fabry-Perot Observation of Optical Maser Output, Bull. Am. Phys. Soc. II, **8**, 1963, p. 380.
5. Kogelnik, H., Imaging of Optical Modes and Resonators with Internal Lenses, to be published.
6. Yariv, A., and Gordon, J. P., The Laser, Proc. IEEE, **51**, 1963, pp. 4-29.
7. Herriott, D. R., Kogelnik, H., and Kompfner, R., Off-Axis Path in Spherical Mirror Interferometers, to be published.
8. Off-axis transmission of modes is discussed in a forthcoming publication by H. E. Rowe.
9. Pierce, J. R., *Theory and Design of Electron Beams*, Princeton, D. van Nostrand, 1954, p. 195.

